

1- عزم العطالة الكتلي المرجع على الحد القائد:

$$J(\varphi_2) = J_2\dot{\varphi}_2^2 + J_3\dot{\varphi}_3^2 + J_6\dot{\varphi}_6^2 + m_{34}r^2\dot{\varphi}_3^2 + (m_{45} + m_5)\dot{X}_5^2$$

$$\dot{\varphi}_2 = \frac{d\varphi_2}{dt} = 1, \quad r_2\varphi_2 = r_3\varphi_3 \Rightarrow \varphi_3 = \frac{r_2}{r_3}\varphi_2 \Rightarrow \dot{\varphi}_3 = \frac{r_2}{r_3} = \frac{0.1}{0.4} = \frac{1}{4} = 0.25$$

$$r_3\varphi_3 = -r_6\varphi_6 \Rightarrow \varphi_6 = -\frac{r_3}{r_6}\varphi_3 = -\frac{r_3}{r_6}\frac{r_2}{r_3}\varphi_2 \Rightarrow \dot{\varphi}_6 = -\frac{r_2}{r_6} = -\frac{0.1}{0.3} = -\frac{1}{3}$$

$$X_5 \cong L + r \cdot \cos \varphi_3 = L + r \cdot \cos \frac{r_2}{r_3}\varphi_2 \Rightarrow \dot{X}_5 = -r \cdot \frac{r_2}{r_3} \sin \frac{r_2}{r_3}\varphi_2 \Rightarrow \dot{X}_5 = -0.2(0.25) \sin \frac{\varphi_2}{4} \quad (6)$$

$$\dot{X}_5 = -0.05 \sin \frac{\varphi_2}{4}$$

$$m_{34} + m_{45} = m_4 = 8. \quad m_{34}l = m_{45}(L - l) \Rightarrow m_{34}(0.2) = m_{45}(0.8 - 0.2) \Rightarrow m_{34} = 3m_{45}$$

$$m_{45} = 2 \text{ kg}, \quad m_{34} = 6 \text{ kg} \quad (4)$$

$$J(\varphi_2) = 0.15 + 0.5(0.25)^2 + 0.4 \left(-\frac{1}{3}\right)^2 + 6(0.2)^2(0.25)^2 + (2 + 10) \left(-0.05 \sin \frac{\varphi_2}{4}\right)^2$$

$$J(\varphi_2) = 0.240694 + 0.03 \sin^2 \left(\frac{\varphi_2}{4}\right)$$

$$J(\varphi_2) = 0.240694 + 0.03 \left(\frac{1 - \cos\left(\frac{\varphi_2}{2}\right)}{2}\right) \Rightarrow J(\varphi_2) = 0.255694 - 0.015 \cos\left(\frac{\varphi_2}{2}\right) \quad (6)$$

$$J(\varphi_2) = J_m \mp \Delta J \Rightarrow \delta_1 = \frac{\Delta J}{J_m} = \frac{0.015}{0.255694} = 0.05866 \quad (2)$$

السؤال الثاني: (22 درجة)

1- حساب عزم مقاومة العمل المرجع على الحد القائد:

$$Q = \sum_{i=2}^n [F_{Xi} \cdot \dot{X}_i + F_{Yi} \cdot \dot{Y}_i + M_i \cdot \dot{\varphi}_i]$$

$$\varphi_2 = 4\varphi_5 \Rightarrow \varphi_5 = \frac{1}{4}\varphi_2 \Rightarrow \dot{\varphi}_5 = \frac{1}{4} = 0.25$$

$$2\pi i = 2\pi \frac{1}{0.25} = 8\pi \text{ دورة العمل}$$

$$M_W = M_5 \times \dot{\varphi}_5 = \begin{cases} 0 & 0 \leq \varphi_2 \leq 2\pi \\ -2400 \times 0.25 = -600 \text{ N} \cdot \text{m} & 2\pi \leq \varphi_2 \leq 4\pi \\ -4800 \times 0.25 = -1200 \text{ N} \cdot \text{m} & 4\pi \leq \varphi_2 \leq 6\pi \\ 0 & \varphi_2 = 8\pi \end{cases} \quad (5)$$

- حساب عزم المحرك الضروري في حالة التشغيل المستقر

$$W_W = -W_M$$

$$W_M = \int_0^{8\pi} M_M d\varphi_2 = 8\pi M_M$$

$$W_W = \int_0^{8\pi} M_W d\varphi_2 = (2\pi)(-600) + (2\pi)(-1200) + \frac{1}{2}(2\pi)(-1200) =$$

$$= -4800\pi = -15079.6447 \text{ [N.m]}$$

$$8\pi M_M = 4800\pi \Rightarrow M_M = \frac{4800}{8} = 600 \text{ [N.m]} \quad (5)$$

$$M_{eq} = \begin{cases} 600 & [N \cdot m] & 0 \leq \varphi_2 \leq 4\pi \\ 0 & [N \cdot m] & 2\pi \leq \varphi_2 \leq 4\pi \\ -600 & [N \cdot m] & 4\pi \leq \varphi_2 \leq 6\pi \\ 600 & [N \cdot m] & \varphi_2 = 8\pi \end{cases}$$

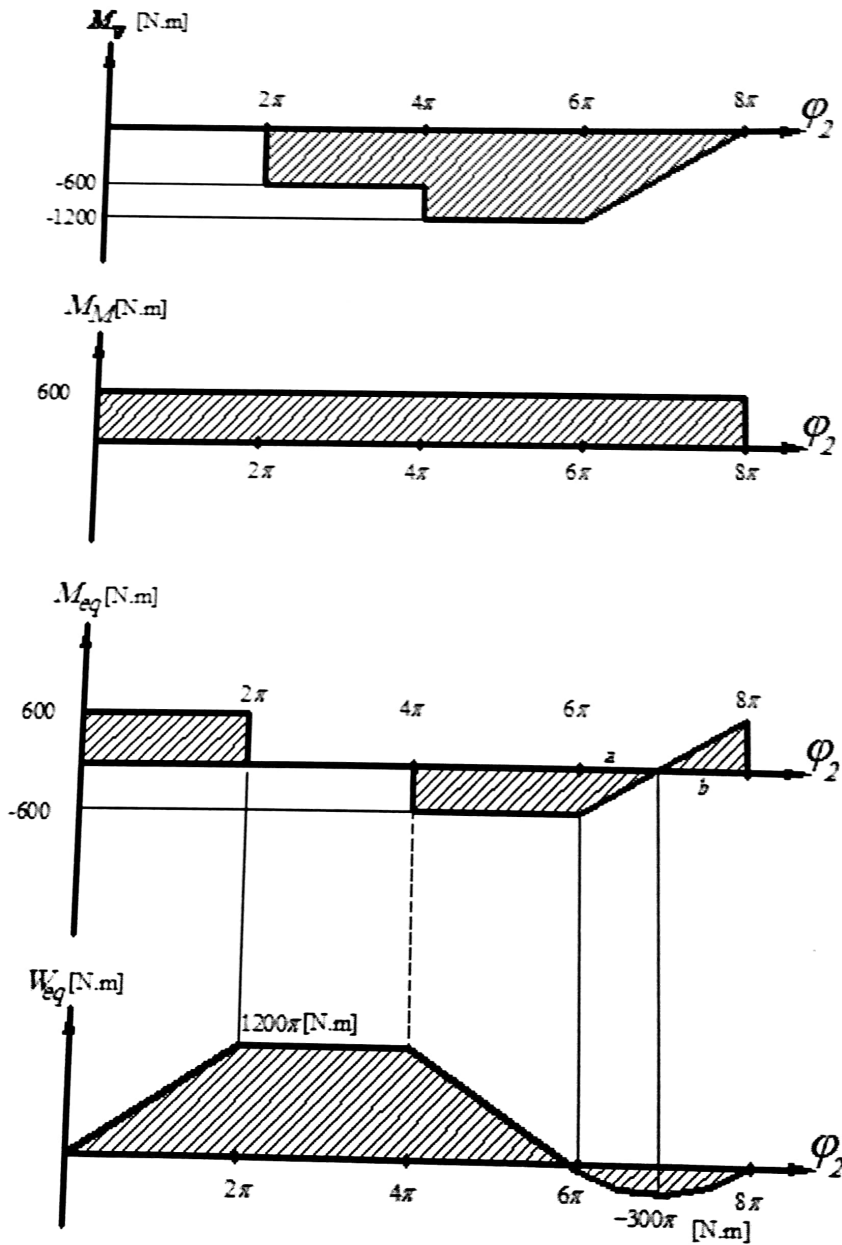
$$a + b = 2\pi, \quad \frac{a}{b} = \frac{600}{600} = 1 \Rightarrow b = a$$

$$a = \pi, \quad b = \pi$$

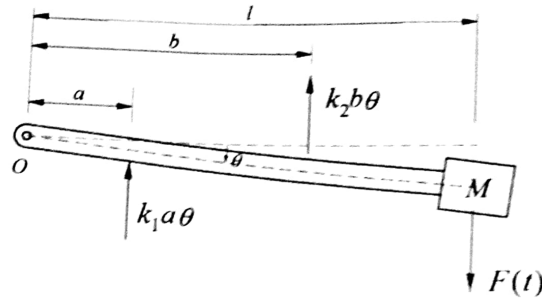
$$W_{max} = \int_0^{2\pi} M_{eq} d\varphi_2 = 600(2\pi) = 1200\pi = 3769.91 [N.m]$$

(8)

$$W_{min} = \int_0^{2\pi} M_{eq} d\varphi_2 = 600(2\pi) - 600(2\pi) - \frac{1}{2}(\pi)(600) \\ = -300\pi = -942.478 [N.m]$$



(4)



(3)

$$\omega = \frac{2\pi(1000)}{60} = \frac{100\pi}{3} = 104.7197551 \left[\frac{\text{rad}}{\text{sec}} \right] \quad (2)$$

المعطيات $J_o = \frac{1}{12}ml^2 + m\left(\frac{l}{2}\right)^2 = \frac{1}{3}ml^2 = \frac{1}{3}(10)(1)^2 = 3.3333 \text{ [kg.m}^2\text{]} \quad (2)$

$$(J_o + Ml^2)\ddot{\theta} = -k_1a^2\theta - k_2b^2\theta + F(t) \times l$$

$$\ddot{\theta} + \frac{k_1a^2+k_2b^2}{J_o+Ml^2}\theta = \frac{F_0l}{J_o+Ml^2}\sin\omega t \Rightarrow \ddot{\theta} + \frac{5000(0.25^2+0.5^2)}{\frac{10}{3}+50(1)^2}\theta = \frac{500(1)}{\frac{10}{3}+50(1)^2}\sin\left(\frac{2\pi(1000)}{60}t\right)$$

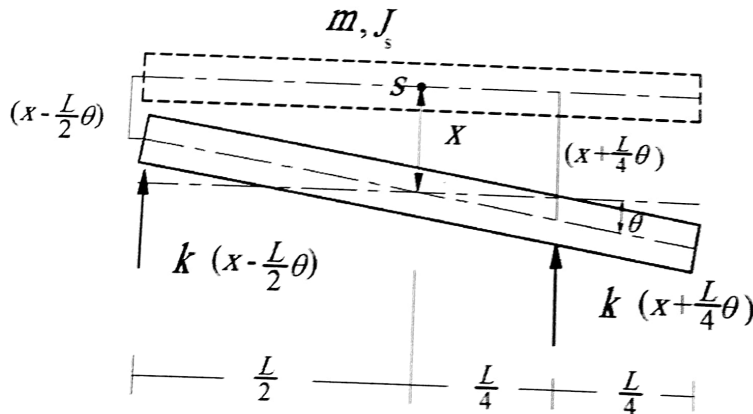
$$\ddot{\theta} + 29.296875\theta = 9.375 \sin \frac{100\pi}{3}t \quad (6)$$

$$\omega_n^2 = 29.296875 \Rightarrow \omega_n = 5.412658774 \left[\frac{\text{rad}}{\text{sec}} \right] \quad (2)$$

$$\theta_{stat} = \frac{\bar{Q}}{\omega_n^2} = \frac{9.375}{29.296875} = 0.32$$

$$\theta = A \sin \omega t \Rightarrow A = \frac{\theta_{stat}}{\sqrt{\left(1 - \left(\frac{\omega}{\omega_n}\right)^2\right)^2}} = \frac{0.32}{\sqrt{\left(1 - \left(\frac{104.7197551}{5.412658774}\right)^2\right)^2}} = 8.571875 \times 10^{-4} \text{ [rad]} \quad (5)$$

السؤال الرابع: (20 درجة)



(4)

$$m\ddot{x} = -k\left(x - \frac{L}{2}\theta\right) - k\left(x + \frac{L}{4}\theta\right) \Rightarrow \ddot{x} + \frac{2k}{m}x - \frac{kL}{4m}\theta = 0 \quad (4)$$

$$J_s\ddot{\theta} = k\left(x - \frac{L}{2}\theta\right)\left(\frac{L}{2}\right) - k\left(x + \frac{L}{4}\theta\right)\left(\frac{L}{4}\right) \Rightarrow \frac{1}{12}ml^2\ddot{\theta} = \frac{kL}{4}x - \frac{5kL^2}{16}\theta \Rightarrow \ddot{\theta} - 3\frac{k}{mL}x + \frac{15k}{4m}\theta = 0 \quad (6)$$

$$a_{11} = \frac{2k}{m} \left[\frac{1}{s^2} \right] \quad a_{12} = -\frac{kL}{4m} \left[\frac{m}{s^2} \right] \quad a_{21} = -3\frac{k}{mL} \left[\frac{1}{m \cdot s^2} \right] \quad a_{22} = \frac{15k}{4m} \left[\frac{1}{s^2} \right] \quad (6)$$

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